

## A MATLAB Script for Predicting Solar Eclipses

This document describes a MATLAB script named `seclipse.m` that can be used to predict local circumstances of solar eclipses. This computer program provides the universal times and topocentric coordinates of the Sun and Moon at the beginning and end of the penumbra contacts, and the time and coordinates at maximum eclipse. The source ephemeris for this routine is a JPL binary ephemeris file. This application uses several functions ported to MATLAB from the Fortran version of the NOVAS (Naval Observatory Vector Astrometry Subroutines) source code developed at the United States Naval Observatory ([www.usno.navy.mil/USNO/astromical-applications/software-products/novas](http://www.usno.navy.mil/USNO/astromical-applications/software-products/novas)). JPL binary ephemeris files for Windows compatible computers can be downloaded at [www.cdeagle.com](http://www.cdeagle.com).

This script uses a combination of one-dimensional minimization and root-finding to solve this classical astronomy problem. The objective function used in these calculations is the difference between the selenocentric (Moon-centered) separation angle between the axis of the lunar shadow and an Earth observer, and the penumbra shadow angle. This function is given by the following expression:

$$f(t) = \cos^{-1}(\hat{\mathbf{u}}_{axis} \cdot \hat{\mathbf{u}}_{m-o}) - \psi_p$$

where

$\hat{\mathbf{u}}_{axis}$  = selenocentric unit vector of the Moon's shadow

$\hat{\mathbf{u}}_{m-o}$  = selenocentric unit position vector of the observer

$\psi_p$  = penumbra shadow angle

The penumbra shadow angle at the distance of the Earth observer is determined from

$$\psi_p = \sin^{-1}\left(\frac{r_m}{d_m}\right) + \sin^{-1}\left(\frac{r_s + r_m}{d_{m-s}}\right)$$

In this expression  $r_m$  is the radius of the Moon,  $r_s$  is the radius of the Sun,  $d_m$  is the topocentric distance of the Moon, and  $d_{m-s}$  is the distance from the Moon to the Sun.

The selenocentric position vector of the Sun is computed from the expression

$$\mathbf{r}_{m-s} = \mathbf{r}_s - \mathbf{r}_m$$

where  $\mathbf{r}_s$  is the geocentric position vector of the Sun and  $\mathbf{r}_m$  is the geocentric position vector of the Moon. The distance  $d_{m-s}$  in the equation above is the scalar magnitude of this vector.

The following is a typical user interaction with this MATLAB script. The screen output created by the script illustrates the local circumstances of a partial solar eclipse. The initial calendar date was December 25, 2000, the search duration was 30 days, and the observer was located at the Chamberlin Observatory in Denver, Colorado. The calendar date and time displayed are on the UTC time scale.

## Celestial Computing with MATLAB

```
local circumstances of solar eclipses
=====
please input an initial UTC calendar date
please input the calendar date
(1 <= month <= 12, 1 <= day <= 31, year = all digits!)
? 12,1,2000
please input the search duration (days)
? 30
please input the geographic latitude of the observer
(-90 <= degrees <= +90, 0 <= minutes <= 60, 0 <= seconds <= 60)
(north latitude is positive, south latitude is negative)
? 39,40,36
please input the geographic longitude of the observer
(0 <= degrees <= 360, 0 <= minutes <= 60, 0 <= seconds <= 60)
(east longitude is positive, west longitude is negative)
? -104,57,12
please input the altitude of the observer (meters)
(positive above sea level, negative below sea level)
? 1644

begin penumbral phase of solar eclipse
-----
calendar date          25-Dec-2000
universal time          15:29:28.878
UTC Julian date         2451904.1455
solar topocentric azimuth angle +132d 09m 24.36s
solar topocentric elevation angle +10d 05m 17.59s
lunar topocentric azimuth angle +132d 10m 25.51s
lunar topocentric elevation angle +10d 36m 24.38s

greatest eclipse conditions
-----
calendar date          25-Dec-2000
universal time          16:43:49.826
UTC Julian date         2451904.1971
solar topocentric azimuth angle +146d 57m 12.48s
solar topocentric elevation angle +19d 22m 51.65s
lunar topocentric azimuth angle +146d 44m 37.17s
lunar topocentric elevation angle +19d 36m 46.75s
```

## Celestial Computing with MATLAB

```
end penumbral phase of solar eclipse
-----
calendar date          25-Dec-2000
universal time          18:06:14.692
UTC Julian date         2451904.2543
solar topocentric azimuth angle +166d 15m 18.44s
solar topocentric elevation angle +25d 42m 22.42s
lunar topocentric azimuth angle +165d 41m 32.92s
lunar topocentric elevation angle +25d 49m 17.46s
event duration          +02h 36m 45.8133s
```

The following are the results for this same eclipse using the Multiyear Interactive Computer Almanac (MICA) published by the United States Naval Observatory.

Solar Eclipse of 2000 Dec. 25  
Sun in Partial Eclipse at this Location  
Delta T: 64.1s

Chamberlin Obs., Denver  
Location: W104°57'12.0", N39°40'36.0", 1644m  
(Longitude referred to Greenwich meridian)

	UT1	Sun's	Position	Vertex
	d h m s	Altitude °	Azimuth °	Angle °
Eclipse Begins	25 15:29:29.6	10.1	132.2	319.7
Maximum Eclipse	25 16:43:36.3	19.4	146.9	
Eclipse Ends	25 18:06:14.6	25.7	166.3	65.6

Duration: 2h 36m 45.0s  
Magnitude: 0.396  
Obscuration: 27.3%